



THE UNIVERSITY *of* EDINBURGH

Edinburgh Research Explorer

Comment on "How to observe coherent electron dynamics directly" Reply

Citation for published version:

Suominen, HJ & Kirrander, A 2014, 'Comment on "How to observe coherent electron dynamics directly" Reply', *Physical Review Letters*, vol. 113, no. 18, 189302. <https://doi.org/10.1103/PhysRevLett.113.189302>

Digital Object Identifier (DOI):

[10.1103/PhysRevLett.113.189302](https://doi.org/10.1103/PhysRevLett.113.189302)

Link:

[Link to publication record in Edinburgh Research Explorer](#)

Document Version:

Publisher's PDF, also known as Version of record

Published In:

Physical Review Letters

Publisher Rights Statement:

Copyright © 2014 American Physical Society. This article may be downloaded for personal use only. Any other use requires prior permission of the author and the American Physical Society.

General rights

Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy

The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact openaccess@ed.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.



Comment on “How to observe coherent electron dynamics directly”

The main results of Ref. [1] rely on the assumption of the validity of Eq. (1) in Ref. [1]. In essence, that equation is meant to establish a connection between the time-dependent electron density of a nonstationary electronic system and the observable x-ray scattering pattern associated with that system. The authors of Ref. [1] claim that their Eq. (1) rests exclusively on the assumption that the electronic dynamics to be imaged are much slower than the duration of the x-ray pulse employed to probe those dynamics. (This is in addition to the assumption of nonresonant x-ray probe conditions.) The purpose of this Comment is to point out that Eq. (1) in Ref. [1] is generally invalid; a short pulse duration is by no means sufficient to guarantee the validity of that equation. An example demonstrating the failure of Eq. (1) in Ref. [1] for an x-ray pulse shorter than the electron dynamics to be imaged may be found in Ref. [2]. Therefore, we consider the validity of the results of Ref. [1] questionable. Particularly, it must be expected that the patterns in Fig. 5 of Ref. [1] differ qualitatively from what would be found in experiment.

Let us assume that the electronic wave packet of interest evolves freely, i.e.,

$$|\Psi_I, t\rangle = \sum_I \alpha_I e^{-iE_I t} |\Psi_I\rangle, \quad (1)$$

where $|\Psi_I\rangle$ is an eigenstate of the electronic Hamiltonian, E_I is the associated eigenenergy, and α_I is a time-independent, generally complex expansion coefficient. In order to make things particularly transparent, let us assume that only two electronic eigenstates— $|\Psi_1\rangle$ and $|\Psi_2\rangle$ —contribute to the wave packet. Then, the expectation value of any observable will oscillate periodically with the period $T = 2\pi/|E_2 - E_1|$. A probe pulse that can resolve these oscillations will necessarily be shorter than T ; equally necessarily, such a pulse has a spectral bandwidth that exceeds the energy splitting between $|\Psi_1\rangle$ and $|\Psi_2\rangle$. This is obvious from Fourier considerations, and it holds irrespective of whether T is a femtosecond or much longer. It is fundamentally impossible to make the spectral bandwidth of the incoming x-ray beam small in comparison to the energy splitting between $|\Psi_1\rangle$ and $|\Psi_2\rangle$ if one is using an x-ray pulse that is short enough to resolve the dynamics associated with coherent superpositions of those electronic eigenstates. It must therefore be expected that even if the x-ray scattering detector has perfect energy resolution (a most optimistic assumption), the scattering signal will involve an incoherent sum over all final states that are energetically accessible within the spectral bandwidth of the incoming x-ray beam. A careful analysis within the framework of quantum electrodynamics demonstrates that this is indeed the case [2], leading, in general, to a failure of Eq. (1) in Ref. [1].

This failure is particularly easy to see if we assume, for simplicity, that the only final states energetically accessible

are $|\Psi_1\rangle$ and $|\Psi_2\rangle$ themselves (a gross oversimplification in view of the nonuniform energy level structure in the Coulomb problem). Then, for a probe pulse much shorter than T , the differential scattering probability per x-ray pulse, at high photon energy, is

$$\frac{dP}{d\Omega} = \zeta \int d^3x \int d^3x' \langle \Psi, t_d | \hat{n}(\mathbf{x}) \times \{ |\Psi_1\rangle \langle \Psi_1| + |\Psi_2\rangle \langle \Psi_2| \} \hat{n}(\mathbf{x}') | \Psi, t_d \rangle e^{i\mathbf{Q} \cdot (\mathbf{x} - \mathbf{x}')} \quad (2)$$

Here, $\hat{n}(\mathbf{x})$ is the electron density operator, \mathbf{Q} is the photon momentum transfer, t_d is the time at which the x-ray probe pulse scatters from the electronic wave packet (the pump-probe time delay), and the constant ζ depends, among other things, on the spectrum of the incoming x-ray beam and on the spectral response of the x-ray scattering detector. Equation (2) may be easily verified by using the results of Ref. [2]. (One may arrive at the same conclusion by applying the analyses of Refs. [3] and [4].) The key point here is that the right-hand side of Eq. (2) *cannot* be written in the form

$$\int d^3x \int d^3x' \langle \Psi, t_d | \hat{n}(\mathbf{x}) | \Psi, t_d \rangle \langle \Psi, t_d | \hat{n}(\mathbf{x}') | \Psi, t_d \rangle e^{i\mathbf{Q} \cdot (\mathbf{x} - \mathbf{x}')} ,$$

which, up to a prefactor, is Eq. (1) from Ref. [1] in the notation employed here. In other words, the requirement of a short pulse—or slow electronic dynamics—does not ensure that the final state reached in the photon collision process equals the electronic wave-packet state right before the collision. Finally, we would like to mention that analogous considerations have been shown to apply to time-resolved electron scattering [5].

R. Santra,^{1,2} G. Dixit³ and J. M. Slowik^{1,2}

¹Center for Free-Electron Laser Science
DESY, Notkestraße 85, 22607 Hamburg, Germany

²Department of Physics, University of Hamburg
Jungiusstraße 9, 20355 Hamburg, Germany

³Max Born Institute
Max-Born-Straße 2 A, 12489 Berlin, Germany

Received 4 March 2014; published 28 October 2014

DOI: 10.1103/PhysRevLett.113.189301

PACS numbers: 32.30.-r, 32.80.Ee, 34.80.Qb, 82.53.Hn

- [1] H. J. Suominen and A. Kirrander, *Phys. Rev. Lett.* **112**, 043002 (2014).
- [2] G. Dixit, O. Vendrell, and R. Santra, *Proc. Natl. Acad. Sci. U.S.A.* **109**, 11636 (2012).
- [3] S. Tanaka, V. Chernyak, and S. Mukamel, *Phys. Rev. A* **63**, 063405 (2001).
- [4] N. E. Henriksen and K. B. Møller, *J. Phys. Chem. B* **112**, 558 (2008).
- [5] H.-C. Shao and A. F. Starace, *Phys. Rev. A* **88**, 062711 (2013).